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Theoretical studies on the stability of salts formed by 3-substituted 6-nitraminotetrazines with different cations

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Abstract A series of energetic salts based on the cations NH_4^+ , NH_3OH^+ , $N_2H_5^+$ and $C(NH_2)_3^+$ and the anions of 6-nitraminotetrazine and its 3-substituted derivatives of -NH₂, -N₃, -ONO₂, -NF₂ or -NO₂ was studied using dispersion-corrected density functional theory (DFT-D). In comparison with salts of unsubstituted 6-nitraminotetrazine, -NH₂ substitution strengthens the hydrogen bonding interaction and other intramolecular interactions (such as charge transfer, binding energy, second-order perturbation energy and dispersion energy), -N3 has tiny effects on these interactions, and other groups weaken these interactions, with weakening decreasing in the order $-NO_2 \ge -NF_2 \ge -ONO_2$. The ability of the cations to produce strong intramolecular interactions decreases in the order $NH_3OH^+ > N_2H_5^+ >$ $NH_4^+ > C(NH_2)_3^+$, which is contrary to the order of the basicity of bases. Stronger intramolecular interactions lead to more stable salts. All substituent groups improved the chemical stability except -ONO2, while cations had no effect on chemical stability. All substituent groups were helpful in improving aromaticity, in the sequence -ONO₂>-NF₂>-NO₂>-NH₂.

Keywords 6-Nitraminotetrazine derivatives · Cation · Intramolecular interactions · Stability · Density functional calculations

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Introduction

In recent years, substantial efforts have been devoted to developing new energetic compounds for various applications, e.g., propellants, explosives, and pyrotechnic fuels. As a unique class of energetic materials, energetic salts have received a lot of attention because of their advantages over nonionic molecules in many aspects, such as their intrinsically low volatility, low vapor pressure, low handling hazard, high thermal stability, high density and energy, and simple synthesis route with low costs [1-6]. The anions in energetic salts are mainly those of HNO₃, HClO₄, $HN(NO_2)_2$ and $HC(NO_2)_3$ [7–10]. However, synthesized salts based on these acids have their respective shortcomings, for example, explosion products of the salts of HClO₄ pollute the environment [11]; ADN (ammonium dinitramide) is easily hygroscopic [12]; HNF (hydrazinium nitroformate) is sensitive to its purity and size [13].

Recently, the anion of 3-amino-6-nitraminotetrazine (ANAT) [14] has captured people's interest [15]. ANAT contains a 1,2,4,5-tetrazine heterocycle. Compounds with 1,2,4,5tetrazine usually have positive heats of formation (HOFs) and high crystal densities, and can release a large amount of N₂ during detonation, which recomends them as energetic materials [15-18]. The nitramino group of ANAT is helpful for improving the oxygen balance (OB) and nitrogen content, which can lead to a high exothermicity in the combustion and detonation processes, and this group enables ANAT to form energetic salts as an acid. Several salts formed by ANAT have been synthesized with excellent yields and purities [15]. The detonation pressures and detonation velocities of these salts were estimated to be 20.90-28.96 GPa and 7.55-8.90 km/s, respectively [15]. Thermal gravimetric analysis (TGA) and differential scanning calorimetry (DSC) studies showed that the decomposition temperatures (T_{ds}) of these salts were 147.7–248 °C, higher than the $T_{\rm ds}$ of the energetic salts ADN (140 °C) [16] and HNF (123 °C) [17]. Thus, salts formed by ANAT have better thermal stability.

The introduction of -NH₂, -N₃, -ONO₂, -NF₂ or -NO₂ groups to organic molecules has great effects on detonation properties, stabilities, and OBs [18, 19]. In order to search for new anions that can form energetic salts with good performance, the -NH₂ group of ANAT was replaced by -N₃, -ONO₂, -NF₂ and -NO₂ groups. For comparison, the unsubstituted 6-nitraminotetrazine was also considered. The anions of 6-nitraminotetrazine and its -NH2, -N3, -ONO2, -NF₂ and -NO₂ substituted derivatives were numbered I-VI, respectively. The cations to pair with these anions came from the bases NH₃, NH₂OH, N₂H₄ and C(NH)(NH₂)₂, i.e., NH₄⁺ (A), NH_3OH^+ (B), $N_2H_5^+$ (C), and $C(NH_2)_3^+$ (D). The salts were named based on their respective cation and anion, e.g., all representive salts with a cation of NH₃ contain A in their name, and with an anion of 3-amino-6-nitraminotetrazine contain II. The structures and names of all title salts are shown in Fig. 1. Our previous studies showed that intramolecular interactions affect the stability of the salt [20-22]. In order to evaluate the effects of different substituent groups and cations on stability, various intramolecular interactions were studied in this work.

Computational details

Calculations were conducted at the B97-D [23]/aug-cc-pvdz level of density functional theory with dispersion corrections (DFT-D). All structures were identified to be local minima without the presence of imaginary frequencies based on vibrational analysis. Natural bond orbital (NBO) [24] analyses were performed at the same level to estimate the second order perturbation energy. The DFT-D3 program was employed to evaluate the dispersion interaction energy between the cation and anion.

Quantum theory of atoms in molecule (QTAIM) analyses were performed using Multiwfn [25] with the input files (.wfn) generated from Gaussian [26]. The characteristics of the bond critical point (BCP) were obtained in terms of the

Fig. 1 Structures of the title salts

electron density ($\rho_{\rm CP}$) and its Laplacian ($\nabla^2 \rho$) at the critical point, the total electron energy density ($H_{\rm BCP}$), the electron potential energy density ($V_{\rm BCP}$), and the Lagrangian kinetic energy ($G_{\rm BCP}$). The relationships between these parameters are shown in Eqs. (1) and (2):

$$\frac{1}{4}\nabla^2 \rho = 2G_{\rm BCP} + V_{\rm BCP} \tag{1}$$

$$H_{BCP} = G_{BCP} + V_{BCP} \tag{2}$$

The hydrogen bonding energy (in a.u.) was obtained using the following relationship proposed by Espinosa et al. [27]:

$$E_H = V_{BCP}/2 \tag{3}$$

 $\rho^{\prime},$ the density without interaction correction, was estimated as follows:

$$\rho' = \frac{M}{V_{\rm m}} \tag{4}$$

$$V_{\rm m} = p V_{\rm cation} + q V_{\rm anion} \tag{5}$$

Where *M* is the molecular molar weight. V_{cation} and V_{anion} are the volumes of the cation and anion defined as that inside an electronic isodensity contour of 0.001 e/bohr³, respectively. *p* and *q* are the numbers of the cation (X) and anion (Y) in the salt $X_p Y_q$, respectively.

The electrostatic potential $V(\mathbf{r})$ created in the space around a molecule by its nuclei and electrons can be estimated by Eq. (6)

$$V(r) = \sum_{A} \frac{Z_{A}}{|R_{A}-r|} \int \frac{\rho(r')dr'}{\langle r'-r \rangle}$$
(6)

 Z_A is the charge on the nucleus A, located at R_A , and $\rho(\mathbf{r})$ is the electronic density of the system. $V(\mathbf{r})$ is a physical observable, which can be determined computationally. The sign of



 $V(\mathbf{r})$ in any region depends on whether the positive contribution of the nuclei or the negative one of the electrons dominates. When $V(\mathbf{r})$ is computed on a molecular surface, it is labelled as $V_{\rm S}(\mathbf{r})$.

$$V_{\rm S,ave}^{+} = \frac{1}{m} \sum_{i=1}^{m} V_{\rm S}^{+}(r_i)$$
⁽⁷⁾

$$V_{\rm S,ave}^{-} = \frac{1}{n} \sum_{j=1}^{n} V_{\rm S}^{-}(r_j)$$
(8)

$$\rho = \alpha_1 \rho' + \beta_1 \left(\frac{V_{\text{S,ave}}^+}{A_{\text{S}}^+}\right) + \gamma_1 \left(\frac{V_{\text{S,ave}}^-}{A_{\text{S}}^-}\right) + \delta_1 \tag{9}$$

Where *i* and *j* are indices, and *m* and *n* are the numbers of sampling points in positive and negative regions, respectively. $A_{\rm S}^+$ indicates the surface area of a cation on which the electrostatic potential is positive and has an average of $V_{\rm S,ave}^+$, $A_{\rm S}^-$ and $V_{\rm S,ave}$ are the corresponding quantities for an anion. α_1 , β_1 , γ_1 and δ_1 came from reference [28].

The lattice energy H_L of the salt $X_p Y_q$ was obtained using Eq. (10):

$$H_{\rm L} = U_{\rm POT} + \left[(n_{\rm X}/2-2)p + (n_{\rm Y}/2-2)q \right] \times RT$$

= $2I \left[\alpha_2 V_{\rm m}^{-1/3} + \beta_2 \right] + \left[(n_{\rm X}/2-2)p + (n_{\rm Y}/2-2)q \right] \times RT$
(10)

$$V_{\rm m} = \frac{M}{\rho N_A} \tag{11}$$

Where *I* is the ionic strength, which here equals 1 [29]. α_2 and β_2 were taken from reference [29]. n_X and n_Y both equal 6 for these title salts [30]. This method has been employed to predict H_L in many studies [22, 29]. V_m is the volume of a single molecule [29], ρ is the density obtained from Eq. (9).

The atomic charges were obtained from Mulliken population analysis. The net charge transfer was determined from the total number of donation and back donation electrons, i.e.,

$$q = CT(Y \rightarrow X) - CT(X \rightarrow Y)$$
(12)

Where $CT(Y \rightarrow X)$ is the charge transfer from anion to cation and $CT(X \rightarrow Y)$ is the charge transfer from cation to anion after considering the electron polarization effect [31]. It is calculated using Multiwfn by conducting extended charge decomposition analysis (ECDA) [31].

The binding energy (E_b) was obtained using the following equation:

$$E_{\rm b} = E_{\rm salt} - E_{\rm cation} - E_{\rm anion} + E_{\rm bsse} \tag{13}$$

 E_{salt} , E_{cation} and E_{anion} are the total energies of salt, cation and anion, respectively. E_{bsse} is the correction for basis set superposition error (BSSE).

Results and discussion

Intramolecular hydrogen bonding interactions

It is well known that hydrogen bonds formed in salts are beneficial to improving stability and density, which in turn enhances the explosive performance of energetic salts [32]. Structures of 24 salts with intramolecular hydrogen bonds are illustrated in Fig. 2. This figure shows that there are two intramolecular hydrogen bonds in the B-D series, while only one in the A series. So the numbers of intramolecular hydrogen bonds are affected only by cations, not anions or substituents. Inspection of Fig. 2 reveals that the N1-H2...N3 hydrogen bonding interaction exists in all these salts, which demonstrates that the nitramino group plays an important role in formation of intramolecular hydrogen bonds. The intramolecular hydrogen bond lengths in Table 1 show that the H2...3 bond lengths are 1.580-1.690 Å for the A-C series while 1.842–1.931 Å for the D series. This implies that the N1–H2 ···N3 hydrogen bonding interactions of the D series are weaker than those of the A-C series. Another intramolecular hydrogen bonding interaction is O4-H5...O6 for the B series and N4-H5...O6 for the C and D series. The H5...O6 distances are 1.667-1.728 Å, 2.266-2.386 Å and 1.816-1.909 Å for series B, C, and D, respectively. The B series has two hydrogen bonds and the H5…O6 distances of the B series are shorter than those of the C and D series, so salts of the B series should possess the strongest hydrogen bonding interactions, and the C series should have the next strongest ones. Although the D series has one more hydrogen bond than the A series, two hydrogen bonds of the D series are obviously longer than those of the A series. So we conjecture that hydrogen bonding interactions of the A series should be stronger than those of the D series. In other words, the abilities of the cations to form intramolecular hydrogen bonds should decrease in the order $NH_{3}OH^{+}>N_{2}H_{5}^{+}>NH_{4}^{+}>C(NH_{2})_{3}^{+}$.

For the A–D series, the H2…N3 bond lengths have the order of II<I<IIII<IV<V<VI (but DIII<DI). Compared with series I, series II has shorter H2…N3, i.e., the –NH₂ group shortens the H2…N3 bond, while the –ONO₂, –NF₂ and – NO₂ groups elongate the H2…N3 bond, with elongations increasing in the order –ONO₂<–NF₂<–NO₂. The effects of



Fig. 2 Structures with intramolecular hydrogen bond paths

the $-N_3$ group on the H2…N3 bonds of various salts are tiny in comparison with those caused by other groups. For example, the absolute values of the differences between the H2…N3 bond lengths of AII–AVI and AI are AIII (0.007 Å)<AII (0.035 Å)<AIV (0.037 Å)<AV (0.058 Å)< AVI (0.066 Å). For series B–D, the variations in H2…N3

bond lengths caused by the N₃ group are also very small (0.002 Å, 0.005 Å and -0.007 Å for BIII, CIII and DIII, respectively). The H5…O6 bond lengths have the order of II <III<IV<V<VI. In a word, these substituent groups have similar effects on the H2…N3 and H5…O6 lengths, i.e., the – NH₂ group shortens these bonds, the –ONO₂, –NF₂ and –NO₂

Table 1 Bond length r (Å) and hydrogen bond energy $E_{\rm H}$ (in kJ mol⁻¹)

		Ι	II	III	IV	V	VI		Ι	II	III	IV	V	VI
A	<i>r</i> (H2…N3)	1.623	1.588	1.63	1.66	1.681	1.689							
	<i>r</i> (H2-N1)	1.096	1.108	1.094	1.085	1.08	1.078							
	$E_{\rm H}$ (N1-H2···N3)	-74.69	-86.16	-72.64	-64.34	-59.09	-57.25							
В	<i>r</i> (N3…H2)	1.624	1.586	1.626	1.651	1.666	1.678	<i>r</i> (H5…O6)	1.695	1.667	1.686	1.71	1.716	1.728
	r(N1-H2)	1.097	1.109	1.097	1.09	1.086	1.083	<i>r</i> (O4-H5)	1.007	1.012	1.009	1.005	1.004	1.003
	$E_{\rm H}({\rm N1-H2\cdots N3})$	-76.03	-88.7	-75.49	-68.57	-64.36	-61.59	$E_{\rm H}({\rm O4}\text{-}{\rm H5}\cdots{\rm O6})$	-48.94	-54.58	-50.62	-46.22	-45.05	-43.18
С	<i>r</i> (N3⋯H2)	1.632	1.597	1.637	1.645	1.645	1.673	<i>r</i> (H5…O6)	2.307	2.266	2.326	2.372	2.372	2.386
	r(N1-H2)	1.093	1.103	1.091	1.088	1.088	1.081	<i>r</i> (N4-H5)	1.028	1.029	1.028	1.025	1.025	1.025
	$E_{\rm H}$ (N1-H2···N3)	-73.22	-84.24	-71.91	-69.01	-61.74	-60.58	$E_{\rm H}$ (N4-H5···O6)	-12.51	-13.81	-12.19	-10.46	-10.17	-10.02
D	<i>r</i> (N3····H2)	1.882	1.842	1.875	1.906	1.917	1.931	<i>r</i> (H5…O6)	1.849	1.816	1.847	1.881	1.894	1.909
	r(N1-H2)	1.035	1.04	1.035	1.032	1.031	1.03	<i>r</i> (N4-H5)	1.032	1.036	1.032	1.029	1.028	1.026
	$E_{\rm H}$ (N1-H2···N3)	-28.69	-32.88	-29.41	-26.58	-25.66	-24.57	$E_{\rm H}$ (N4-H5···O6)	-29.88	-33.19	-29.91	-27.14	-26.11	-24.85

groups elongate these bonds in sequence, and the $-N_3$ group has tiny effects on these bonds.

BCPs and paths of intramolecular hydrogen bonds of all salts produced from QTAIM are shown in Fig. 2. The hydrogen bond energies $(E_{\rm H}s)$ of these salts are listed in Table 1. Parameters ($\rho_{CB} \nabla^2 \rho$, $V_{BCB} G_{BCP}$ and H_{BCP}) related to BCP are supplied in Table S1 as supporting information. The absolute values of $\rho_{\rm CP}$, $\nabla^2 \rho$, $V_{\rm BCP}$, $G_{\rm BCP}$ and $E_{\rm H}$ increase with the decrease in hydrogen bond length. This implies that these parameters are sensitive to hydrogen bond length. Therefore, these parameters can be regarded as indicators of the strength of the hydrogen bond. According to the identification rule of hydrogen bond proposed by Rozas et al. [33] (i.e., $\nabla^2 \rho > 0$ and $H_{\rm BCP} > 0$ for weak hydrogen bonds, $\nabla^2 \rho > 0$ and $H_{\rm BCP} < 0$ for medium and strong hydrogen bonds, and $\nabla^2 \rho < 0$ and $H_{BCP} < 0$ for very strong ones), the hydrogen bonds of A and B series salts are all strong, the salt of C series has one strong and one weak hydrogen bond, and the salt of D series has two weak hydrogen bonds. The total hydrogen bond energies $E_{\rm H,tot}$ s (Table 3) of the salts with the same anion follow the order of B>C>A>D. In light of the results of hydrogen bond strengths and $E_{\rm H,tot}$ of salts with the same anion, we conclude that the ability to form hydrogen bonds of these cations is NH₃OH⁺> $N_2H_5^+ > NH_4^+ > C(NH_2)_3^+$. This order is the same as that obtained from the bond lengths and opposite to that of basicity (pK_b) of the corresponding bases [34]: D (0.29)>A (4.79)>C (5.9)>B (8.03), i.e., the cation of the weaker base has a stronger ability to form hydrogen bonds. This is because the weaker base results in weaker attraction between the proton and base, which is helpful for the proton to form a hydrogen bond with the anion.

The absolute values of the H2…N3 hydrogen bond energy of salts with the same cation are in the order II>I>III>IV> V>VI (but DIII>DI) wh, ich is totally contrary to the order of the H2…N3 bond lengths. The effects of all groups except $-N_3$ on the H2...N3 hydrogen bond energy are obvious. For the A series, the $-NH_2$ group improves this energy by 15 % $(=\frac{E_{\rm H}(\rm AII)-E_{\rm H}(\rm AI)}{F_{\rm er}(\rm AI)}$), while –ONO2, –NF2, –NO2 and –N3 de- $E_{\rm H}({\rm AI})$ crease it by 14 %, 24 %, 30 % and 2 %, respectively. In comparison with AI, -NH₂, -N₃, -ONO₂, -NF₂ and -NO₂ groups change the H2…N3 length by only -2.16 %, 0.4 %, 2.27 %, 3.49 % and 3.93 %, respectively. So $E_{\rm H}$ is more sensitive to the substituent group than is the hydrogen bond length. For series B-D, the variations in the H2…N3 hydrogen bond energy caused by these groups are similar to those of the A series. For the H5…O6 hydrogen bond energies of series B–D, the –NH₂ group improves these energies by 10– 12 %, the -ONO₂, -NF₂ and -NO₂ groups decrease these energies by 6-16 %, 8-19 % and 12-20 %, respectively. The - N_3 group changes this energy by only 3 %, -3 % and 0 for the B, D and D series, respectively. The absolute values of $E_{\rm H,tot}$ s of salts with the same cation are in the order II>I>III>IV>

V>VI (but DIII>DI), i.e., the $-NH_2$ group improves $E_{H,tot}$, while the $-ONO_2$, $-NF_2$ and $-NO_2$ groups decrease $E_{H,tot}$ in sequence, and the $-N_3$ group has only a tiny effect on $E_{H,tot}$.

It is well known that hydrogen bonds are helpful in improving the stability of salts, and previous investigations have shown that stronger hydrogen bond interactions are tightly correlated to higher stability of the salt [32, 22]. According to the above conclusions, the order of the ability to improve the stability of the salts is $NH_3OH^+ > N_2H_5^+ > NH_4^+ > C(NH_2)_3^+$ for cations and $-NH_2 > -H > -N_3 > -ONO_2 > -NF_2 > -NO_2$ for substituents.

Other intramolecular interactions

The second-order perturbation energy (E_2) from orbital interactions is usually called the stabilization energy. In this paper, E_2 s between the lone pairs LP(N3), LP(N6) or LP(O6) of anions and the $\sigma^*(N1-H2)$ or $\sigma^*(N4-H5)$ of cations were evaluated and the results are listed in Table 2. E_2 s from the different orbital interactions of the salts with the same cation generally have the order of II>I>III>IV>V>VI. Just like the effects on $E_{\rm H}$ s, E_2 s are improved by the $-NH_2$ group, while successively decreased by the $-ONO_2$, $-NF_2$ and $-NO_2$ groups. The effect of the $-N_3$ group is slight; the largest deviation caused by the $-N_3$ group is only 1.29 kcal mol⁻¹.

 E_{2} s of LP(N3) $\rightarrow \sigma^{*}(N1-H2)$ of series A–C salts with the same anion are comparable (the largest deviation is about 2.9 kcal mol^{-1}) and are obviously larger than the corresponding values of the D series (the least deviation between the D series and series A–C is 23.59 kcal mol^{-1}). This phenomenon should be related to the fact that the H2…N3 bond lengths of series A-C salts with the same anion are close to each other and are distinctly smaller than those of the D series (for example, the H2…N3 bond lengths are 1.623 Å, 1.624 Å, 1.632 Å and 1.882 Å for AI–DI, respectively). The E_{2} s of LP(N6) $\rightarrow \sigma^*(O4-H5)$ of C series salts are obviously smaller than the corresponding values of series B and D, which is consistent with the fact that the H5…N6 bond lengths of the C series are obviously larger than those of the B and D series. In light of these conclusions, E_2 should be tightly related with the hydrogen bond length. Therefore, the relationships between the H···N or H···O length and the corresponding E_{2} s were fitted, and the quadratic relationships found. The results are shown in Fig. 3. This figure clearly shows that E_2 s gradually decreases with elongation of the hydrogen bond.

The total second-order perturbation energies ($E_{2,tot}$ s) of all salts are listed in Table 3. $E_{2,tot}$ s of the salts with the same cation have the order II>I>III>IV>V>VI, and $E_{2,tot}$ s of the salts with the same anion decrease in the order B>C>A>D. A previous study reported that a larger $E_{2,tot}$ between the ions results in more stable compounds [22]. Therefore, it can be concluded that the abilities of groups to improve the stability of salts have the order of $-NH_2 > -H > -N_3 > -ONO_2 > -NF_2 > -$

Table 2 Orbital interactions and second-order perturbation energy $(E_2, \text{ in kcal mol}^{-1})$

	AI	AII	AIII	AIV	AV	AVI
$E_2(LP(N3) \rightarrow \sigma^*(N1-H2))$	50.91	57.53	49.62	44.49	41.15	39.85
	BI	BII	BIII	BIV	BV	BVI
$E_2(LP(N3) \rightarrow \sigma^*(N1-H2))$	49.86	56.64	49.21	45.09	42.55	40.84
$E_2(LP(O6) \rightarrow \sigma^*(O4-H5))$	25.75	28.97	26.64	23.97	23.23	22.14
	CI	CII	CIII	CIV	CV	CVI
$E_2(LP(N3) \rightarrow \sigma^*(N1-H2))$	49.55	55.29	48.60	47.39	40.99	42.67
$E_2(LP(N6) \rightarrow \sigma^*(O4-H5))$	2.54	3.02	2.29	1.23	1.06	1.17
	DI	DII	DIII	DIV	DV	DVI
$E_2(LP(N3) \rightarrow \sigma^*(N1-H2))$	19.62	22.49	20.14	17.90	17.15	16.26
$E_2(LP(N6) \rightarrow \sigma^*(O4-H5))$	16.25	18.89	16.17	14.36	13.47	12.21

NO₂, and the contributions of cations to the second-order perturbation energies decrease in the order of $NH_3OH^+ > N_2H_5^+ > NH_4^+ > C(NH_2)_3^+$.

In order to comprehensively elucidate the influences of different substituent groups and different cations on the intramolecular interactions between the cation and anion, the charge transfer, binding energy, dispersion energy and lattice energy were estimated. The energies of the frontier orbitals are also listed in Table 3. The variations of these parameters are plotted in Fig. 4.

The energies released upon formations of salts by the isolated ions are reflected in the E_{b} s values. A larger E_{b} means greater stabilization of the ions after formation of the salt. When the cation is the same, anions with the $-NH_2$ group give the largest E_{b} s, and anions with $-N_3$ and -H lead to very similar E_{b} s. The E_{b} s of salts with $-ONO_2$, $-NF_2$ and $-NO_2$ groups are smaller than those of the salts in I series. In other words, the stabilization of anions with different substituents follows the order $-NH_2 > -H > -N_3 > -ONO_2 > -NF_2 > -NO_2$, when they form salts with the same cation, and stabilization of cations follows the order $NH_3OH^+ > N_2H_5^+ > NH_4^+ > C(NH_2)_3^+$ when they form salts with the same anion.

The values of q and E_{dis} of salts with the same cation have similar variation trends: II>I \approx III>IV>V>VI, i.e., these interactions are strengthened by the $-NH_2$ group, while weakened by the $-ONO_2$, $-NF_2$ and $-NO_2$ groups in sequence. The $-N_3$ group has hardly any obvious effect on these interactions. Briefly, the intramolecular interactions of salts with the same cation and the same anion follow the order II>I \approx III>IV>V> VI and B>C>A>D, respectively. In addition, the values of q obtained from NBO analysis (listed in Table S2) exhibit the same variation trends as that from Mulliken analysis.

Figure 4 shows that the variation trends of q, $E_{2,tot}$, E_{b} , E_{dis} and $E_{\rm H,tot}$ of salts with the same cation are similar, which may imply that relationships exist between these parameters. Therefore, the relationships between q and $E_{2,tot}$, E_b , E_{dis} and $E_{\rm H tot}$ were fitted. Herein, only the fitted results of the B series are shown (Fig. 5) since they are similar for series A-D. As seen in Fig. 5, linear relationships exist between q and $E_{2,\text{tot}}, E_{b}, E_{\text{dis}}$ and $E_{\text{H,tot}}$, and in fact a linear relationship exists between any two of them. This means that these intramolecular interactions are tightly related to each other. It is well known that the larger E_2 and E_H may lead to a more stable salt [22]. According to the above discussion, the larger E_2 and $E_{\rm H}$ also correspond to stronger intramolecular interactions, which may in turn result in a more stable salt. Therefore, the stabilities of salts with the same cation and the same anion have the order of II>I≈III>IV>V>VI and B>C>A>D, respectively.

For salts with the same cation, H_L s values follow the order I>II>VI>V>III>IV, i.e., all substituents decrease H_L . H_L s of salts with the same anion have the order of A>B>C>D. According to Eq. (10), H_L is determined mainly by the volume and type of salt. All title salts are of the XY type, i.e., the ratio of the number of cations to anions is 1:1. So the cationic and







Table 3 Predicted total second-order perturbation energies $(E_{2,\text{tot}})$, lattice energy (H_L) , binding energy (E_b) , dispersion energy (E_{dis}) , total hydrogen bond energies $(E_{\text{H,tot}})$, energy of the highest occupied

molecular orbitals (E_{HOMO}), energy of the lowest unoccupied molecular orbitals (E_{LUMO}), chemical stability (E_{g}) and net charge transfer (q) of all salts under investigation

Compound	<i>q</i> (e)	$E_{2,\text{tot}}$ (kcal mol ⁻¹)	$E_{\rm b}$ (kcal mol ⁻¹)	$E_{\rm dis}$ (kcal mol ⁻¹)	$E_{\rm H,tot} ({\rm kcal} {\rm mol}^{-1})$	$H_{\rm L}$ (kcal mol ⁻¹)	$E_{\rm HOMO}({\rm eV})$	$E_{\rm LUMO}({\rm eV})$	$E_{\rm g}({\rm eV})$
AI	0.251	50.91	-113.96	-3.86	-74.69	126.94	-4.96	-3.19	1.77
AII	0.275	57.53	-120.78	-3.90	-86.16	123.93	-4.83	-2.94	1.89
AIII	0.250	49.62	-111.17	-3.85	-72.64	121.11	-5.21	-3.39	1.82
AIV	0.234	44.49	-105.17	-3.76	-64.34	119.25	-5.17	-3.67	1.51
AV	0.225	41.15	-102.65	-3.69	-59.09	121.63	-5.45	-3.60	1.85
AVI	0.221	39.85	-99.91	-3.70	-57.25	121.91	-5.59	-3.69	1.90
BI	0.345	75.61	-132.21	-5.31	-124.97	124.84	-5.31	-3.56	1.75
BII	0.371	85.61	-140.46	-5.35	-143.28	121.90	-5.17	-3.28	1.89
BIII	0.345	75.85	-129.68	-5.29	-126.11	119.30	-5.55	-3.75	1.80
BIV	0.329	69.06	-123.77	-5.26	-114.79	117.57	-5.48	-3.94	1.55
BV	0.318	65.78	-120.75	-5.20	-109.41	119.78	-5.82	-4.02	1.80
BVI	0.311	62.98	-117.52	-5.18	-104.77	120.04	-5.91	-4.06	1.85
CI	0.279	52.09	-117.08	-5.09	-85.73	123.84	-5.05	-3.28	1.77
CII	0.303	58.31	-124.25	-5.20	-98.05	121.01	-4.94	-3.05	1.89
CIII	0.275	50.89	-114.30	-5.13	-84.1	118.50	-5.31	-3.50	1.81
CIV	0.264	48.62	-107.72	-4.91	-79.47	116.83	-5.17	-3.67	1.50
CV	0.247	42.05	-105.42	-4.85	-71.91	118.96	-5.55	-3.71	1.84
CVI	0.248	43.84	-101.98	-4.76	-70.6	119.21	-5.58	-3.70	1.88
DI	0.259	35.87	-99.12	-5.13	-58.57	119.16	-4.64	-2.87	1.77
DII	0.278	41.38	-105.13	-5.22	-66.07	116.82	-4.55	-2.66	1.89
DIII	0.259	36.31	-97.03	-5.15	-59.32	114.70	-4.93	-3.12	1.81
DIV	0.244	32.26	-91.78	-5.07	-53.72	113.28	-4.86	-3.43	1.43
DV	0.237	30.62	-89.92	-5.00	-51.77	115.10	-5.16	-3.32	1.84
DVI	0.230	28.47	-87.31	-4.93	-49.42	115.30	-5.25	-3.42	1.83

anionic volumes are the only influence factors. The substituent groups naturally increase the volumes of anions, and the larger anionic volume certainly results in the smaller $H_{\rm L}$, so the lattice energies of series II–VI salts are all smaller than those of the I series. The order of cationic volumes is $\rm NH_4^{+<}$ $NH_3OH^+ < N_2H_5^+ < C(NH_2)_3^+$, which naturally results in the opposite order of H_Ls for salts with the same anion.

Inspection of Table 3 reveals that the energies of the highest occupied molecular orbitals (E_{HOMO} s) and the lowest unoccupied molecular orbitals (E_{LUMOs}) of series II–VI salts with the



Fig. 4 Variations in net charge transfer (q), total second-order perturbation energies $(E_{2,tot})$, binding energy (E_b) , dispersion energy (E_{dis}) , lattice energy (H_L) and chemical stability (E_g)



Fig. 5 Relationships between q and $E_{2,tot}$, E_b , E_{dis} and $E_{H,tot}$



Fig. 6 Highest occupied molecular orbitals (HOMOs, top) and lowest unoccupied molecular orbitals (LUMOs, bottom) of series II

same cation are obviously different from those of the I series. This implies that these groups have distinct effects on HOMOs and LUMOs. The order of E_g generally is II>VI>V>III>I>IV, i.e., all substituent groups except $-ONO_2$ are helpful for



Fig. 7 Orbital interaction diagram of AI. Solid lines Occupied orbitals, dashed lines virtual orbitals

improving E_g , i.e., chemical stability. It is worth noting that salts with the same anion have very close E_g s (for example, the E_g s of AIII–DIII are 1.82 eV, 1.80 eV, 1.81 eV and 1.81 eV, respectively), so the effects of different cations on E_g are negligible. In view of the fact that E_g is determined mainly by the anion, HOMO and LUMO should be contributed from that anion. This is verified by the 3D frontier orbital distributions shown in Fig. 6. Since all salts have similar frontier orbital distributions, only those of series II are shown. Obviously, HOMOs and LUMOs are cderived from ompletely anions, cations make hardly any contribution to these frontier orbitals. In addition, the shapes of HOMOs and LUMOs of the salts with the same anion are almost the same, with different cations having hardly any effects.

The contributions of the orbitals of isolated ions to the frontier orbitals of the salts can be seen clearly in orbital interaction diagrams. Since all the salts here have similar orbital interaction diagrams, only that of AI is shown (Fig. 7). The orbital interaction diagram shows that the HOMO (the highest solid line) and LUMO (the lowest dashed line) of the salt are both contributed from the HOMO and LUMO of the anion in the isolated state. The frontier orbitals of the isolated cation make no contribution. The occupied and vacant orbitals of the individual anion correspond to the corresponding occupied and vacant orbitals are conserved when the individual ions form salts according to the Woodward-Hoffman rule [35].

Aromaticity

Aromaticity is an important concept in physical organic chemistry [36, 37]. It is useful in the rationalization of structure,

Table 4	Values of nucleus-
independ	lent chemical shifts
(NICS)(1)zzs (in ppm) of all salts

	Ι	Π	III	IV	V	VI
А	-10.0230	-13.5312	-20.0748	-21.3985	-20.4782	-20.2531
В	-5.2529	-7.4579	-18.8560	-26.1249	-21.3279	-20.5292
С	-5.3284	-7.8117	-19.8001	-24.7078	-19.6265	-18.8899
D	-2.4981	-8.1969	-9.5252	-25.8049	-12.1491	-11.6217

stability, and reactivity of molecules. However, because of its multiple manifestations, as yet there there is no generally accepted quantitative definition of aromaticity. Among the many indexes of aromaticity, a magnetic criterion, nucleusindependent chemical shifts (NICS) [38] is most widely used due to its simplicity and efficiency. An earlier study [39] showed that NICS(1)ZZ, i.e., the NICS calculated at the point 1 Å above (or below) the ring center, is a better index than the original definition of NICS, known as NICS(0). Here, the NICS(1)_{ZZ}s of these salts were estimated at the B3LYP/6-31+G*//B97D/aug-cc-pvdz level. The definition of the ring center was highly arbitrary, with the geometry or mass center being used first. Use of the ring critical point (RCP) of AIM (atoms in molecule) theory as the ring center has also been recommended [40]. In this paper, the RCPs were estimated using Multiwfn and used as the ring centers. Multiwfn was also employed to calculate $NICS(1)_{77}$.

The calculated NICS(1)_{ZZ}s (Table 4) of these salts are all negative, i.e., they are all aromatic [38]. Previous studies [38, 41] revealed that the more negative the NICS(1)_{ZZ}, the stronger the aromaticity of the compound. The aromaticities of A–D series salts follow the order of IV>V>VI>III>III>II>I, which means that these groups are helpful in improving aromaticity.

The ability to improve aromaticity is strongest for the $-ONO_2$ group, and for other groups it decreases gradually in the order $-NF_2 \ge -NO_2 \ge -N_3 \ge -NH_2$. The effects of cations on aromaticity are not coincident. Generally speaking, salts with NH_4^+ have the strongest aromaticity, and those of the salts with NH_3OH^+ and $N_2H_5^+$ are comparable.

The atoms of substituents that connect directly with the tetrazine ring and participate in delocalization may improve the aromaticity of the ring. Figure 8 shows the delocalized bonds between the ring and the substituents of AI-AVI. The delocalized bonds of a salt are numbered as bond (1) and bond (2) (see Fig. 8). The lengths of bond (1) of AI-AVI are 1.367, 1.386, 1.369, 1.354, 1.348 and 1.343 Å, respectively. The C-N and C=N bond lengths of CH_3NH_2 and CH_2NH are 1.476 and 1.280 Å at the same level, respectively. So the lengths of bond (1) of the A series are between those of the C-N and C= N bonds, i.e., this bond is delocalized. And the delocalization degree has the order of AVI>AV>AIV>AI>AIII>AII. The order is generally in agreement with the order of the ability of electron-withdrawing of the substituent groups [42], which means that the stronger electron-withdrawing ability of the substituent group leads to the more delocalized bond (1). The lengths of bond (1) of AI and AIII are very similar, i.e., the -



Fig. 8 Structures of AI-AVI with delocalized bonds

 N_3 group has little effect on this bond. Bond (2) is the C–N bond for AII, AIII, AV and AVI and the C–O bond for AIV. The lengths are 1.357, 1.400, 1.451 and 1.483 Å in AII, AIII, AV and AVI, respectively, so the delocalization gradually weakens and in AVI it is actually localized. The delocalization of the C–N bonds in AII and AIII is much more obvious, so their aromaticities are stronger than that of AI. The length of bond (2) of AIV is 1.330 Å, which is smaller than that (1.437 Å) of CH₃OH and larger than that (1.214 Å) of CH₂O. So the delocalization of bond (2) in AIV is large, which is very helpful in improving the aromaticity of AIV and leads to the aromaticity of AIV being stronger than that of AV and AVI.

Conclusions

The ability of substituent groups to improve hydrogen bonding interactions decreases in the order $-NH_2 > -H\approx -N_3 > ONO_2 > -NF_2 > -NO_2$. The abilities of cations to form hydrogen bonds follow the order $NH_3OH^+ > N_2H_5^+ > NH_4^+ >$ $C(NH_2)_3^+$. The effects of substituent groups and cations on the other intramolecular interactions are same as on the hydrogen bonding interactions. Linear relationships exist between *q*, $E_{2,tot}$, E_b , E_{dis} and $E_{H,tot}$. Stronger intramolecular interactions lead to more stable salts. The stabilities of salts with the same cation and the same anion are in the order II>I \approx III>IV>V>VI and B>C>A>D, respectively.

All substituents except $-ONO_2$ improve E_g , and cations have no effect on frontier orbital distribution and E_g . All substituents improve aromaticity, following the order $-ONO_2 \ge -NF_2 \ge -NO_2 \ge -NH_2$.

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